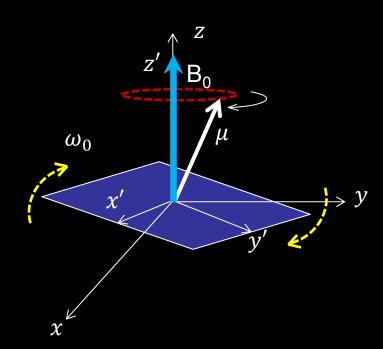
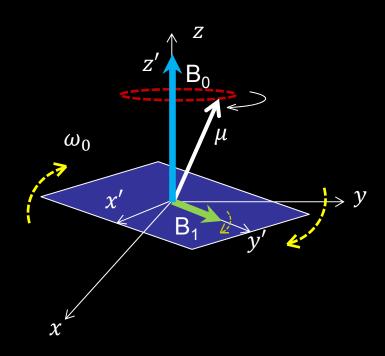
BME-7710 - Magnetic Resonance Imaging

# Chapter 8 – Signal acquisition Methods



#### A rotating B<sub>1</sub> field - ON

... circularly polarized



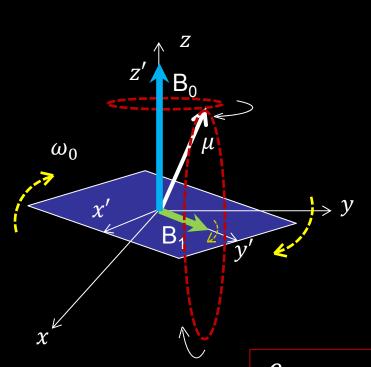
**Resonance Condition** 

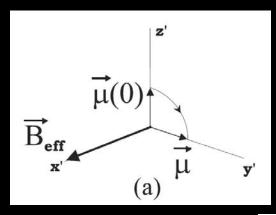
$$\omega' = \omega_0 = -\gamma \cdot B$$

$$\omega_0 = -\gamma \cdot B_0$$

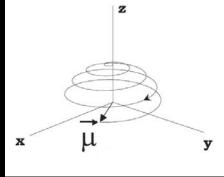
Larmor Frequency

#### A rotating B<sub>1</sub> field - ON





$$\omega_1 = -\gamma \cdot B_1$$



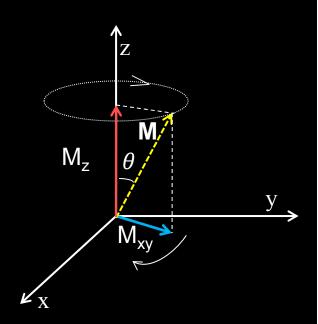
$$\theta = \omega_1 \cdot \tau = -\gamma \cdot B_1 \cdot \tau$$

### Relaxation effects

$$\frac{d\vec{M}}{dt} = \gamma \cdot \vec{M} \times B + \frac{M_0 - M_z}{T_1} - \frac{M_{xy}}{T_2}$$

 $M_0$  is the equilibrium magnetization

 $M_{xy}$  is the transverse magnetization

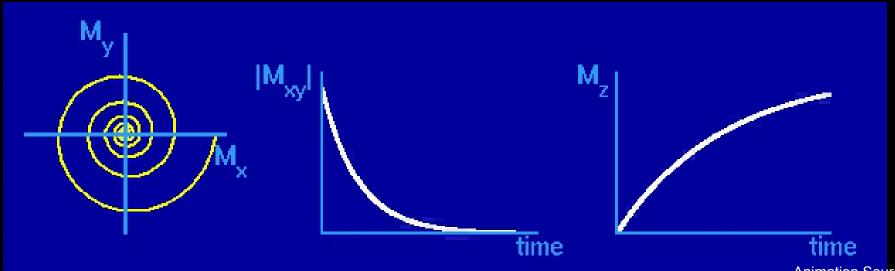


#### Relaxation effects

Transverse Magnetization Decay Longitudinal Magnetization Recovery

$$M_{xy}(t) = M_{xy}(0) \cdot e^{-\frac{t}{T_2}}$$

$$M_z(t) = M_z(t=0) \cdot e^{-\frac{t}{T_1}} + M_0 \cdot \left(1 - e^{-\frac{t}{T_1}}\right)$$



# Basic Contrast Mechanisms: Relaxation effects

Longitudinal Magnetization - Recovery

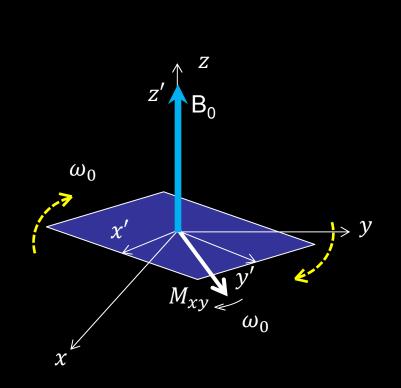
$$M_z(t) = M_z(t=0) \cdot e^{-\frac{t}{T_1}} + M_0 \cdot \left(1 - e^{-\frac{t}{T_1}}\right)$$

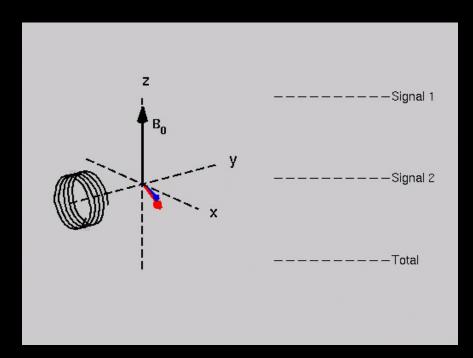
 $T_1$  is the time it takes the magnetization to recover to 63.2% of its equilibrium value  $M_0$ .

$$M_{xy}(t) = M_{xy}(0) \cdot e^{-\frac{t}{T_2}}$$

 $T_2$  is the time it takes the transverse magnetization to decays to 36.7% of its initial value  $M_{xy}$ .

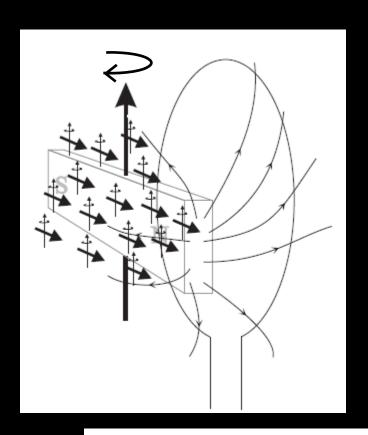
#### A rotating B<sub>1</sub> field - OFF





### Signal Detection

Faraday's Law of Electromagnetic induction



$$emf = -\frac{d\Phi}{dt}$$

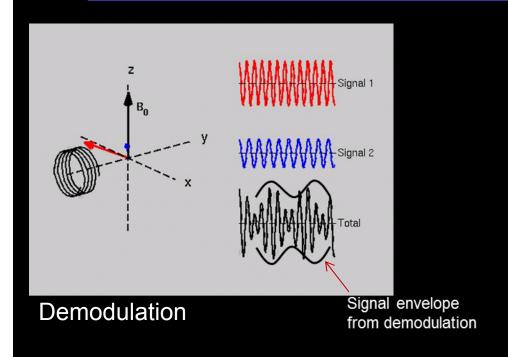
Induced signal is proportional to rate of change of flux

$$\omega_0 = -\gamma \cdot B_0$$

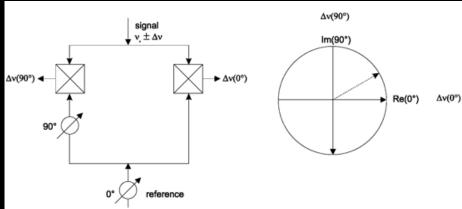
$$\Rightarrow emf \propto \omega_0$$

$$s(t) \propto \omega_0 \int d^3r e^{-t/T_2(\vec{r})} \mathcal{B}_{\perp}(\vec{r}) \underline{M_{\perp}(\vec{r},0)} e^{i(\underline{(\Omega-\omega(\vec{r}))t+\phi_0(\vec{r})-\theta_B(\vec{r})})}$$

# Signal Demodulation and quadrature detection



Quadrature detection or phase sensitive detection:



Quadrature detection allows us to record both x and y components of the transverse magnetization

#### **Key Points in Chapter 8**

- Free Induction Decay
- Spin Echo
- Repeated rf pulse structures –
   Magnetization and signal equations for different rf pulse structures

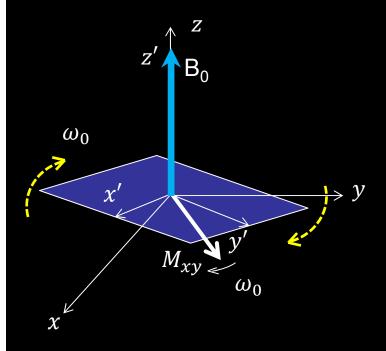
Introducing sequence timing diagram

### Demodulated Signal

$$s(t) \propto \omega_0 \int d^3r e^{-t/T_2(\vec{r})} \mathcal{B}_{\perp}(\vec{r}) M_{\perp}(\vec{r}, 0) e^{i\underline{((\Omega - \omega(\vec{r}))t + \phi_0(\vec{r}) - \theta_{\mathcal{B}}(\vec{r}))}}$$

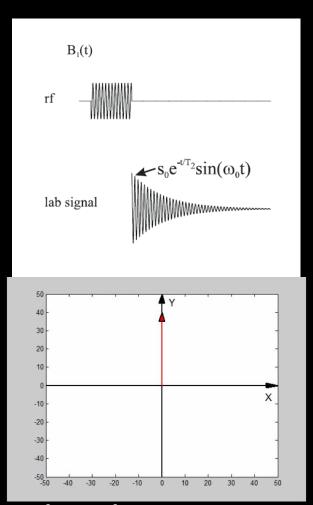
Dropping spatial dependence of T2...

$$s(t) \propto \omega_0 e^{-t/T_2} e^{i((\Omega - \omega_0)t + \phi_0 - \theta_B)} \int d^3r \mathcal{B}_{\perp}(\vec{r}) M_{\perp}(\vec{r}, 0)$$



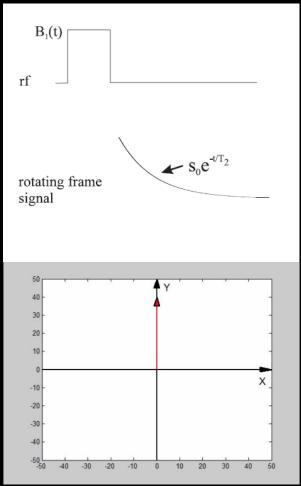
Let's assume uniform coil reception field and magnetization in the sample...

### Demodulation



Laboratory reference frame

#### Demodulated signal



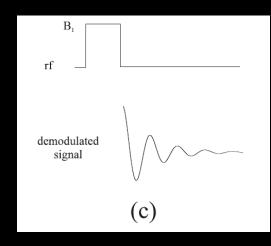
Rotating reference frame

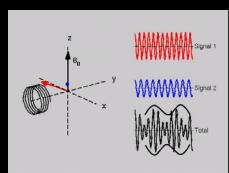
$$M_{xy} = M_0 \cdot e^{-\frac{t}{T_2}}$$

### Free induction decay

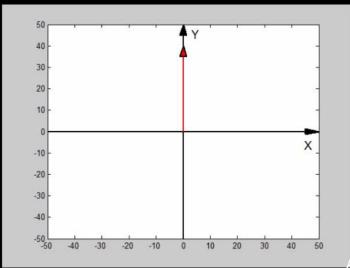
$$s(t) \propto \omega_0 e^{-t/T_2} e^{i((\Omega - \omega_0)t + \phi_0 - \theta_B)} \int d^3r \mathcal{B}_{\perp}(\vec{r}) M_{\perp}(\vec{r}, 0)$$

#### $\Omega \neq \omega_0 \text{ Or } \omega \neq \omega_0$





Signal envelope from demodulation



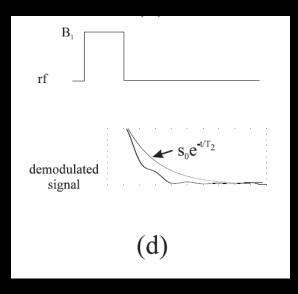
Animation Source:

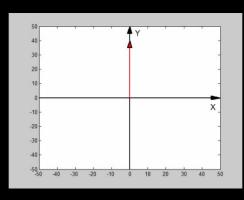
Dr. Yongquan Ye, WSU

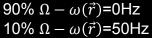
### Free induction decay

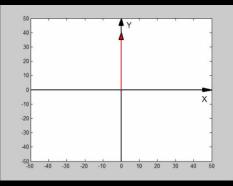
Practical issue: local & global field inhomogeneity exist

$$S(t) = S_0 \int e^{-t/T_2} e^{i(\Omega - \omega(\vec{r}))t} + \phi_0$$

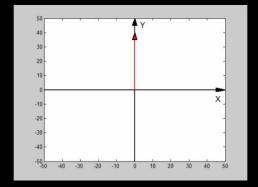








75% 
$$\Omega - \omega(\vec{r}) = 0$$
Hz  
25%  $\Omega - \omega(\vec{r}) = \pm 50$ Hz  
40 spins

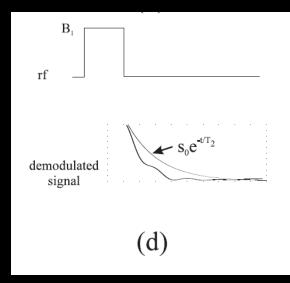


75%  $\Omega - \omega(\vec{r})$ =0Hz 25%  $\Omega - \omega(\vec{r})$ =±50Hz 40,000 spins

### $T_2^*$ and $T_2'$

Practical issue: local & global field inhomogeneity exist

$$S(t) = S_0 \int e^{-t/T_2} e^{i(\Omega - \omega(\vec{r}))t} + \phi_0$$



$$\frac{1}{T_2^*} = \frac{1}{T_2} + \frac{1}{T_2'}$$

Faster decay of signal from transverse magnetization occurs due the presence of local field inhomogeneities

The additional decay time constant is empirically given by  $T_2'$  $(1/T_2' = R_2')$  is the additional relaxation rate

$$M_{xy} = M_0 \cdot e^{-\frac{t}{T_2^*}}$$

$$1/T_2^* = R_2^*$$

$$1/T_2 = R_2^*$$

### $T_2'$

Practical issue: local & global field inhomogeneity exist

$$S(t) = S_0 \int e^{-t/T_2} e^{i(\Omega - \omega(\vec{r}))t} + \phi_0$$

The additional decay rate,  $T'_2$ , could be estimated by:

$$e^{-\frac{t}{T_2'}} \sim \int e^{i(\Omega - \omega(\vec{r}))t}$$

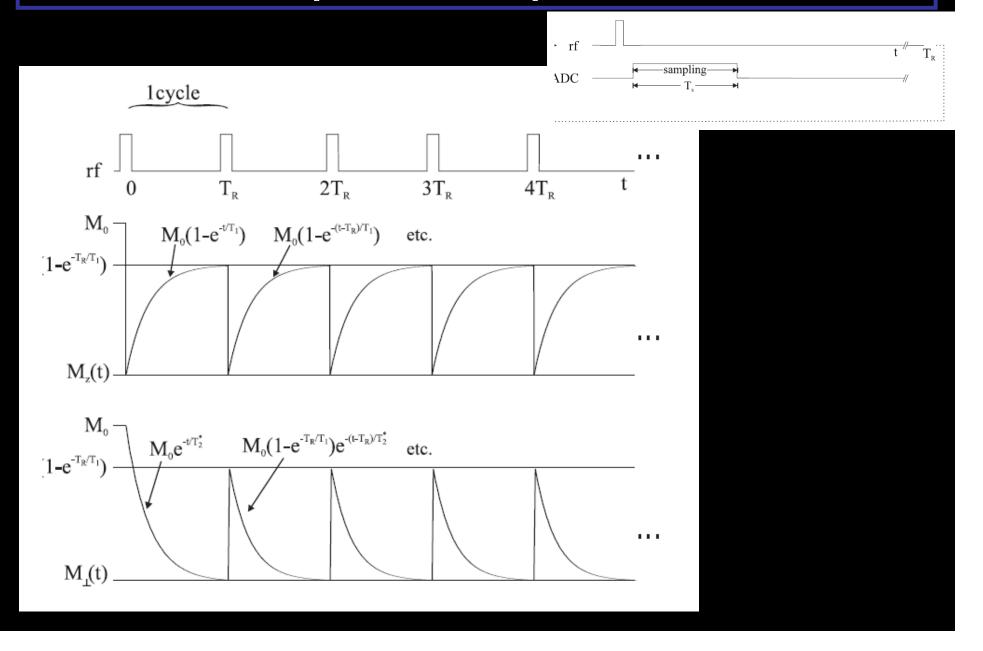
$$\varphi(r,t) = (\Omega - \omega(r)) \cdot t + \phi_0$$

$$\varphi(r,t) = \gamma (B_0 - B(r)) \cdot t + \phi_0 \qquad \qquad \varphi(r,t) = \gamma (B_0 - (B_0 + \Delta B(r))) \cdot t + \phi_0$$

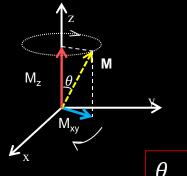
$$\varphi(r,t) = -\gamma \cdot \Delta B(r) \cdot t + \phi_0$$

$$e^{-\frac{t}{T_2'}} \sim \int e^{i\varphi(r,t)}$$

### Multi-pulse experiments



### Magnetization equations



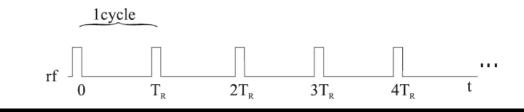
$$M_z(t) = M_z(0) \cdot e^{-\frac{t}{T_1}} + M_0 \cdot \left(1 - e^{-\frac{t}{T_1}}\right)$$
  $M_{xy}(t) = M_{xy}(0) \cdot e^{-\frac{t}{T_2^*}}$ 

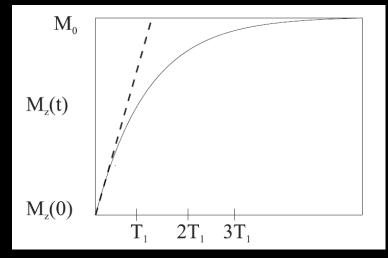
$$M_z(0) = M_0 \cdot \cos(\theta)$$

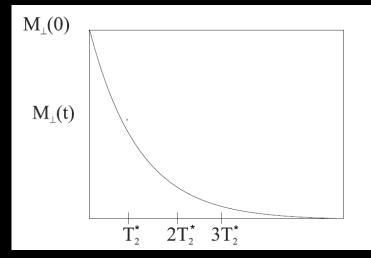
$$M_{xy}(t) = M_{xy}(0) \cdot e^{-\frac{t}{T_2^*}}$$

$$M_{xy}(0) = M_0 \cdot \sin(\theta)$$

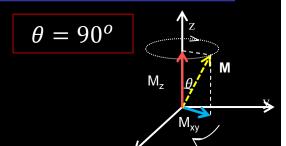








### FID sampling and repeated scans



With a 90° excitation:

$$\begin{cases} M_Z(0^+) = 0 \\ M_\perp(0^+) = M_0 \end{cases}$$

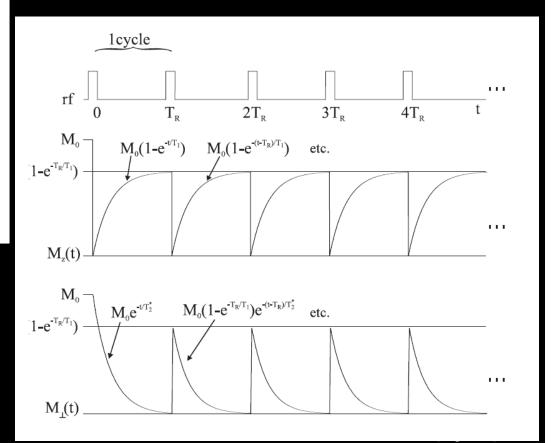
$$\begin{cases} M_z(TR^-) = M_0(1 - e^{-TR/T1}) \\ M_\perp(TR^-) = M_0e^{-TR/T_2^*} \end{cases}$$

:

$$\begin{cases} M_Z(nTR^-) = M_0(1 - e^{-TR/T1}) \\ M_\perp(nTR^-) = M_0(1 - e^{-TR/T1})e^{-TR/T_2^*} \end{cases}$$

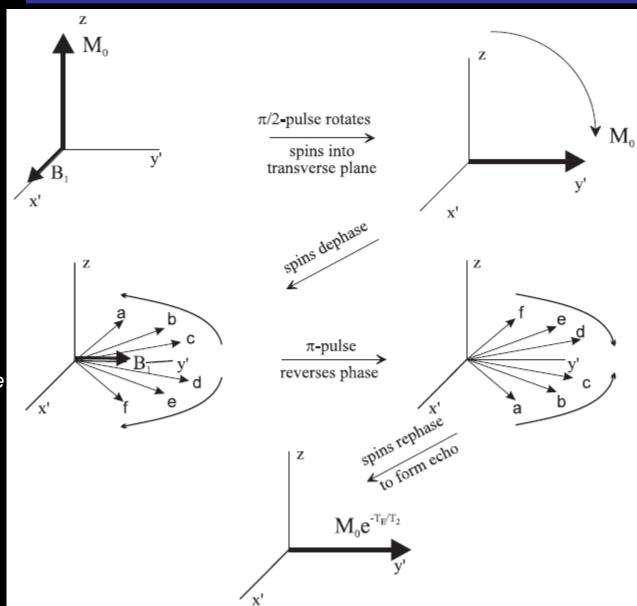
Note that both T1 and T2\* affect the signal's amplitude

 $TR \gg T_2^*$ 

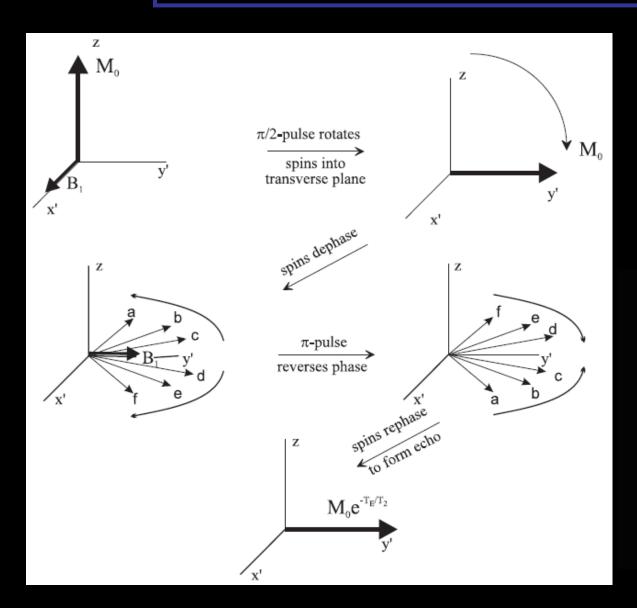


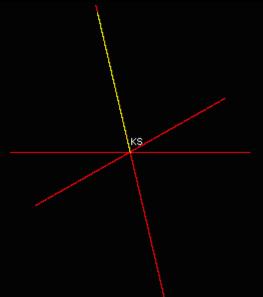
 $\pi/2$  rf pulse about the x' axis

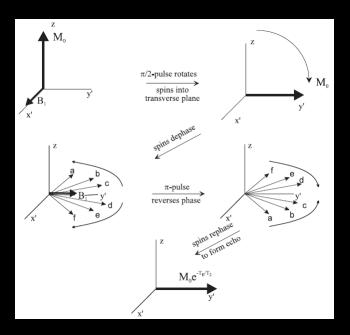
 $\pi$  refocusing rf pulse about the y' axis

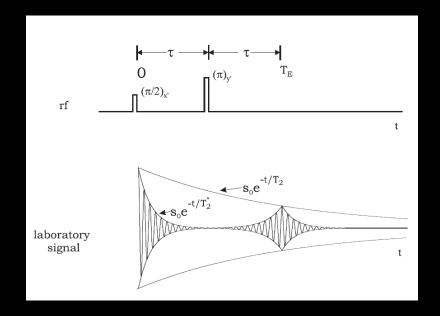


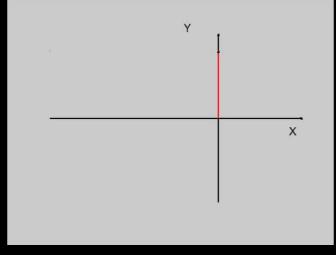
Echo occurs along the y' axis











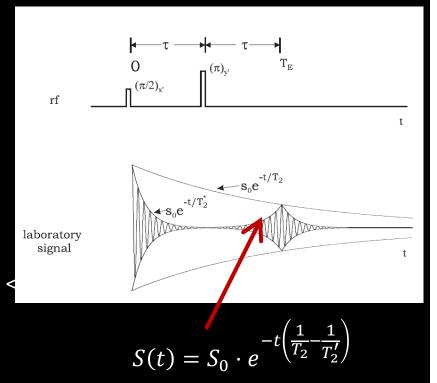
#### How SE works

1. 
$$\phi(\vec{r},t) = -\gamma \Delta B(\vec{r})t$$
,  $0 < t < \tau$ 

Refocusing  $\pi$  pulse after time  $\tau$ ...

2. 
$$\phi(\vec{r}, \tau^+) = -\phi(\vec{r}, \tau^-) = \gamma \Delta B(\vec{r}) \tau, t = \tau$$

3. 
$$\phi(\vec{r},t) = -\gamma \Delta B(\vec{r})(t-\tau) + \gamma \Delta B(\vec{r})\tau$$
,  $\tau < t < \tau$ 



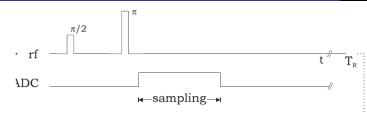
4. 
$$\phi(\vec{r}, 2\tau) = 0, t = 2\tau \equiv TE$$

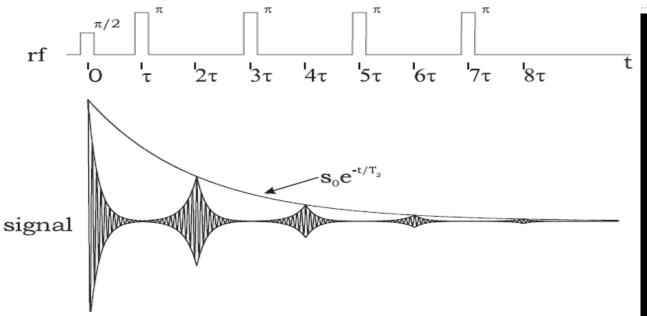
5. 
$$\phi(\vec{r},t) = -\gamma \Delta B(\vec{r})(t-2\tau,t) > 2\tau$$

 $T_2^*$  dephasing continues...

#### Multi-echo Spin Echo







$$S(TE_1) = S_0 \cdot e^{-\frac{TE_1}{T_2}}$$

$$S(TE_2) = S_0 \cdot e^{-\frac{TE_2}{T_2}}$$

$$T_2 = \frac{TE_2 - TE_1}{\ln\left(\frac{S(TE_1)}{S(TE_2)}\right)}$$

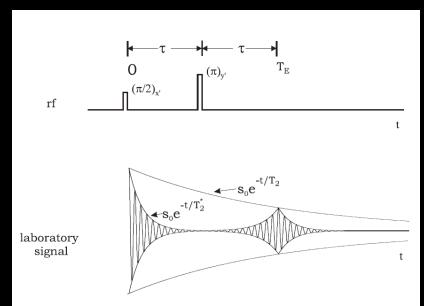
#### Note:

The phase of refocusing pulses greatly affects the signal of ME-SE. Consider the following rf pulse schemes:

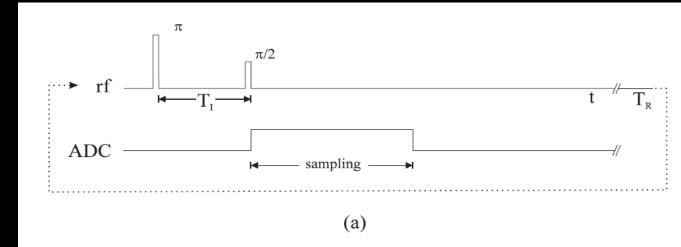
- 1)  $90^{\circ}(x) 170^{\circ}(y) 170^{\circ}(y) 170^{\circ}(y) 170^{\circ}(y) \dots$
- 2)  $90^{\circ}(x) 170^{\circ}(y) 170^{\circ}(-y) 170^{\circ}(y) 170^{\circ}(-y) \dots$  (CPMG seq)

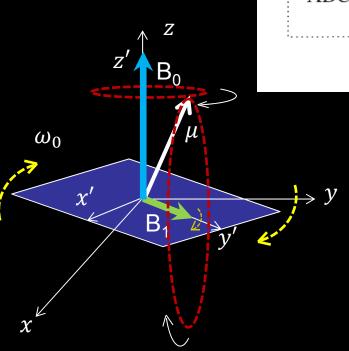
#### **T2**

- Maximal signal limited to T2 decay which is not recoverable
- T2' decay on both sides of the echo acts as low pass filter, blurring the image (Chap. 13)
- True T2 is difficult for precise quantification
  - Motion, partial volume effects, RF pulse, data acquisition, etc.
- Extra consideration for multiple spin echo acquisition
  - RF pulse phase
  - RF energy deposition
  - Multiple signal pathways  $(TR < T_2^*)$
- Long scan time

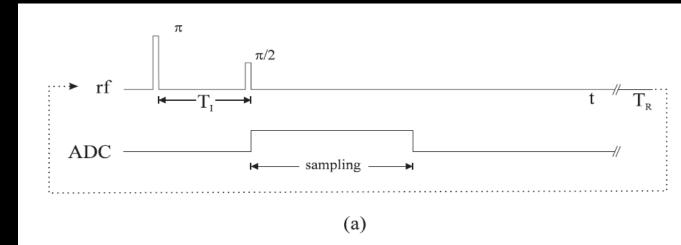


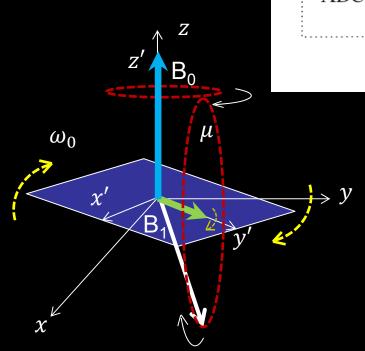
$$M_z(t) = M_z(t=0) \cdot e^{-\frac{t}{T_1}} + M_0 \cdot \left(1 - e^{-\frac{t}{T_1}}\right)$$



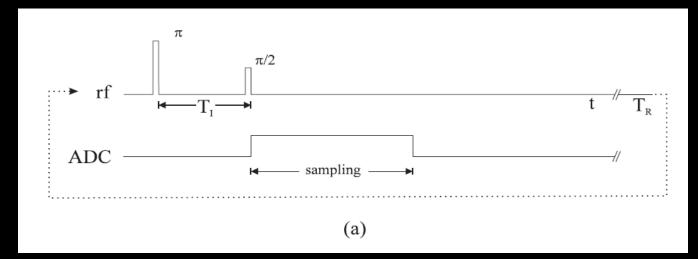


$$M_z(t) = M_z(t=0) \cdot e^{-\frac{t}{T_1}} + M_0 \cdot \left(1 - e^{-\frac{t}{T_1}}\right)$$





$$M_Z(t) = M_Z(t=0) \cdot e^{-\frac{t}{T_1}} + M_0 \cdot \left(1 - e^{-\frac{t}{T_1}}\right)$$



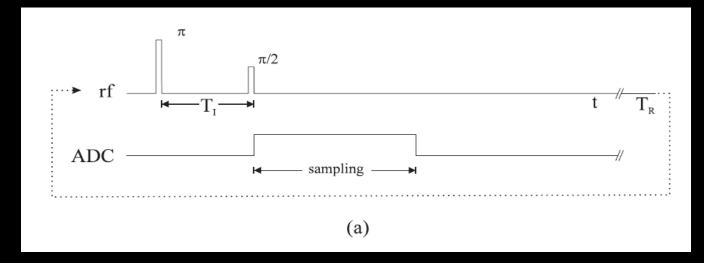
$$M_z(0^+) = -M_0$$

$$M_z(t) = -M_0 e^{-t/T_1} + M_0 (1 - e^{-t/T_1}) = M_0 (1 - 2e^{-t/T_1})$$

$$0 < t < T_I$$

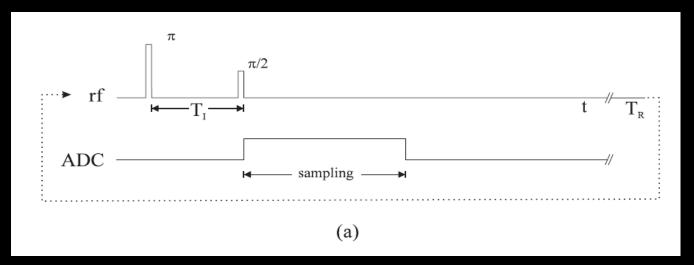
$$M_{\perp}(t) = \left| M_0(1 - 2e^{-T_I/T_1}) \right| e^{-(t-T_I)/T_2^*}, \quad t > T_I$$

$$M_Z(t) = M_Z(t=0) \cdot e^{-\frac{t}{T_1}} + M_0 \cdot \left(1 - e^{-\frac{t}{T_1}}\right)$$



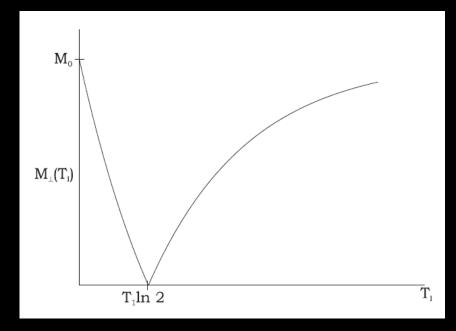
$$M_{\perp}(t) = \left| M_0(1 - 2e^{-T_I/T_1}) \right| e^{-(t-T_I)/T_2^*}, \quad t > T_I$$

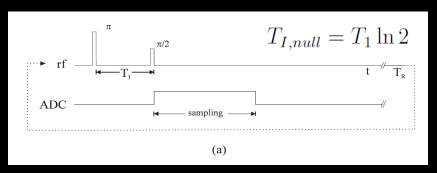
$$T_{I,null} = T_1 \ln 2$$



$$T_{I,null} = T_1 \ln 2$$

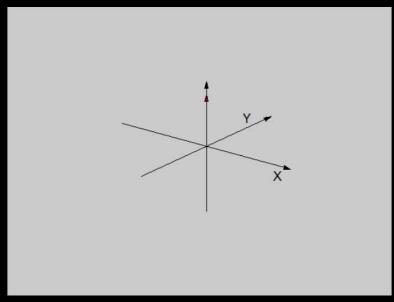
By sampling the signal at varying TIs (inversion time),  $T_1$  of a tissue could be quantified



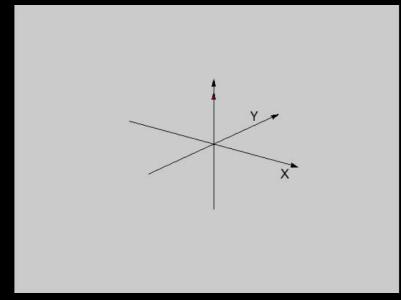


Can also be used to null the signal from a tissue by appropriately timing the  $\pi/2$  pulse if the T1 of the tissue is known

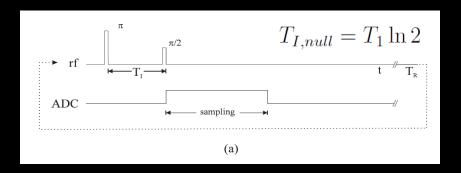
T1=300/1000ms



TI=100ms

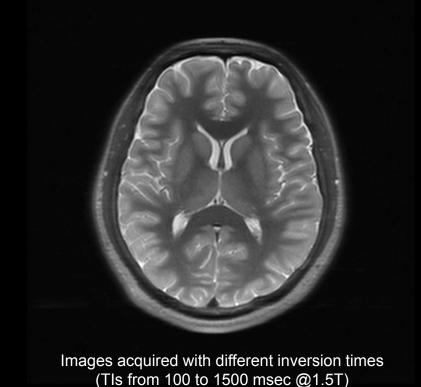


TI=208ms

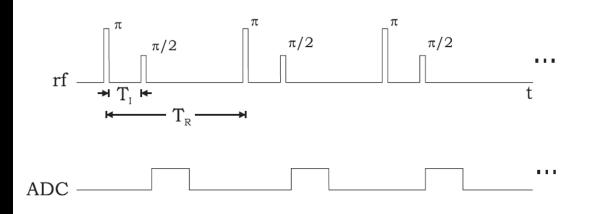


Can also be used to null the signal from a tissue by appropriately timing the  $\pi/2$  pulse if the T1 of the tissue is known

T1=300/1000ms



# Repeated IR scans

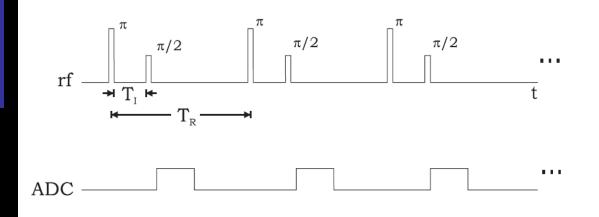


$$M_z(0^+) = -M_z(0^-) = -M_0$$
  
 $M_\perp(0^+) = 0$ 

$$M_z(t) = -M_z(0^-)e^{-t/T_1} + M_0(1 - e^{-t/T_1}) = M_0(1 - 2e^{-t/T_1})$$
  
 $M_\perp(t) = 0$   
 $0 < t < T_I$ 

$$M_z(T_I^+) = 0$$
  
 $M_\perp(T_I^+) = \left| -M_z(0^-)e^{-T_I/T_1} + M_0(1 - e^{-T_I/T_1}) \right| = |M_0(1 - 2e^{-T_I/T_1})|$ 

# Repeated IR scans



$$M_{z}(t) = M_{0} \left( 1 - e^{-(t-T_{I})/T_{1}} \right)$$

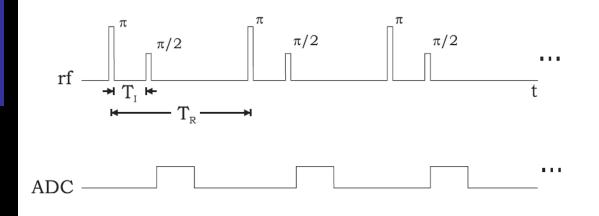
$$M_{\perp}(t) = \left| -M_{z}(0^{-})e^{-T_{I}/T_{1}} + M_{0}(1 - e^{-T_{I}/T_{1}}) \right| e^{-(t-T_{I})/T_{2}^{*}}$$

$$= \left| M_{0}(1 - 2e^{-T_{I}/T_{1}}) \right| e^{-(t-T_{I})/T_{2}^{*}}$$

$$T_{I} < t < T_{R}$$

$$M_z(T_R^-) = M_0 \left(1 - e^{-(T_R - T_I)/T_1}\right)$$

# Repeated IR scans



$$M_{\perp}(t_n) = \left| -M_0(1 - e^{-(T_R - T_I)/T_1})e^{-T_I/T_1} + M_0(1 - e^{-T_I/T_1}) \right| e^{-(t_n - T_I)/T_2^*}$$

$$= M_0 \left| 1 + e^{-T_R/T_1} - 2e^{-T_I/T_1} \right| e^{-(t_n - T_I)/T_2^*}$$

$$T_I < t_n < T_R$$

$$T_{I} = T_1 \ln \left( \frac{2}{1 + e^{-T_R/T_1}} \right)$$

#### Homework

• Prob. 8.1-8.5

**Next Class** 

**Chapter 9.1-9.4**